



# Regular/irregular polygon

Mana Maths

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# Te reo Māori terms



**taparau rite**

regular polygon

Open in Te Aka

**taparau**

polygon

Open in Te Aka

**koki roto**

interior angle

Open in Te Aka

**āhua**

shape

Open in Te Aka

# Regular/irregular polygon — Foundation

1. State whether each polygon is regular or irregular: a pentagon with all sides equal and all angles equal.
2. State whether each polygon is regular or irregular: a hexagon with equal sides but one angle different from the others.
3. State whether each polygon is regular or irregular: a quadrilateral with angles  $90^\circ$ ,  $90^\circ$ ,  $90^\circ$ , and  $90^\circ$  but side lengths 3 cm and 5 cm.
4. Complete the sentence: in a regular polygon, all sides are the same length and all interior angles are equal.
5. Find the sum of the interior angles of a triangle.
6. Find the interior-angle sum of a quadrilateral.
7. Find the sum of the interior angles of a pentagon using  $180(n - 2)$ .
8. Find the sum of the interior angles of a hexagon using  $180(n - 2)$ .
9. Find the sum of the interior angles of an octagon using  $180(n - 2)$ .

- 10.** A regular pentagon has five equal interior angles. Find one interior angle.
- 11.** A regular hexagon has six equal interior angles. Find one interior angle.
- 12.** A regular octagon has eight equal interior angles. Find one interior angle.
- 13.** An irregular pentagon has interior angles  $100^\circ$ ,  $120^\circ$ ,  $110^\circ$ ,  $140^\circ$ , and  $x^\circ$ . Find  $x$ .
- 14.** An irregular hexagon has interior angles  $120^\circ$ ,  $140^\circ$ ,  $130^\circ$ ,  $150^\circ$ ,  $110^\circ$ , and  $x^\circ$ . Find  $x$ .

# Regular/irregular polygon — Proficient

1. A polygon has all sides equal and all interior angles equal. Explain why it must be regular.
2. A polygon has six equal sides but its interior angles are not all equal. Is it regular or irregular? Explain briefly.
3. Find the sum of the interior angles of a heptagon.
4. Find the sum of the interior angles of a nonagon.
5. The sum of the interior angles of a polygon is  $1260^\circ$ . How many sides does the polygon have?
6. The sum of the interior angles of a polygon is  $1440^\circ$ . How many sides does the polygon have?
7. Find one interior angle of a regular decagon.
8. Find one interior angle of a regular nonagon.
9. An irregular pentagon has angles  $95^\circ$ ,  $115^\circ$ ,  $130^\circ$ ,  $140^\circ$ , and  $x^\circ$ . Find  $x$ .

**10.** An irregular hexagon has angles  $x^\circ$ ,  $125^\circ$ ,  $135^\circ$ ,  $145^\circ$ ,  $155^\circ$ , and  $160^\circ$ . Find  $x$ .

**11.** A regular polygon has each interior angle equal to  $135^\circ$ . Name the polygon.

**12.** A regular polygon has each interior angle equal to  $150^\circ$ . How many sides does it have?

# Regular/irregular polygon — Excellence

1. The sum of the interior angles of a polygon is  $(180n - 360)^\circ$ . Explain what the  $n$  represents.
2. A polygon has interior-angle sum  $1620^\circ$ . Find the number of sides.
3. A regular polygon has each interior angle  $156^\circ$ . Find the number of sides.
4. A regular polygon has each interior angle  $165^\circ$ . Find the number of sides.
5. An irregular hexagon has five interior angles of  $118^\circ$ ,  $132^\circ$ ,  $147^\circ$ ,  $151^\circ$ , and  $160^\circ$ . Find the sixth angle.
6. An irregular octagon has seven interior angles of  $120^\circ$ ,  $140^\circ$ ,  $150^\circ$ ,  $135^\circ$ ,  $160^\circ$ ,  $145^\circ$ , and  $155^\circ$ . Find the eighth angle.
7. The interior angles of a regular polygon add to  $1980^\circ$ . Find the polygon and one interior angle.
8. A regular polygon has interior angles of  $140^\circ$  each. Is this possible? Explain using the interior-angle formula.
9. An irregular pentagon has angles in the ratio  $2 : 3 : 3 : 4 : 6$ . Find the five angles.

- 10.** An irregular hexagon has angles in the ratio  $3 : 4 : 5 : 5 : 6 : 7$ . Find the six angles.
- 11.** A regular polygon has one interior angle of  $x^\circ$ . Write a formula for the sum of all interior angles in terms of  $x$  and the number of sides  $n$ .
- 12.** A student says, "If all the angles in a polygon are equal, the polygon must be regular." Give a counterexample or explain why the claim is incomplete.
- 13.** A regular polygon has twice as many sides as a regular pentagon. Find its interior-angle sum and one interior angle.
- 14.** A polygon has 10 sides. Four interior angles are  $140^\circ$ , three are  $150^\circ$ , two are  $160^\circ$ , and one angle is  $x^\circ$ . Find  $x$ .
- 15.** A regular polygon has one interior angle that is  $24^\circ$  more than the interior angle of a regular hexagon. Find the polygon.