



# Nets

Mana Maths

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# Notes – Nets of 3D shapes



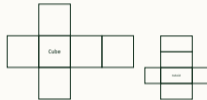
## Key idea

A net is a flat 2D plan that folds along edges to make a 3D shape. The same 3D shape can have many different nets. All faces must be present and connected.

## Steps to identify a net

1. Count the faces. Does the net have the right number? (Cube = 6, cuboid = 6, pyramid = 5, tetrahedron = 4)
2. Check shapes match. Are the faces the correct polygons?
3. Visualise folding. Imagine bending each face along the edge.
4. Check overlaps. No faces should overlap when folded.
5. Check gaps. There should be no gaps between faces.

## Common nets



A cube has 11 distinct nets. A cuboid also has a net of 6 rectangles (3 pairs of equal size).

## Common mistake

Thinking any 6 connected squares form a cube net. In fact, if a cross arm is more than 2 squares long, it won't fold correctly.

# Notes – Nets and surface area



## Example 1: Cube net

A cube of side 3 cm has net area =  $6 \times (3 \times 3) = 54 \text{ cm}^2$ . The net is the surface area of the cube.

## Example 2: Cuboid box

A  $5 \times 3 \times 2$  cm box:  $SA = 2(5 \cdot 3 + 5 \cdot 2 + 3 \cdot 2) = 62 \text{ cm}^2$ .

## Example 3: Opposite faces

In a cube cross net, the two squares at the ends of the cross are opposite each other when folded.

## Example 4: Open box

An open box net has 5 faces (no top). Its surface area excludes the missing top face.

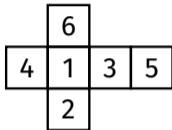
## Try these

1. Draw a cube net of side 2 cm.
2. Find surface area of a 4 cm cube.
3. Identify opposite faces in a cross net.

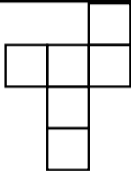
## Common mistake

Forgetting that opposite faces never share an edge in a net. In the cross net, the top and bottom squares are opposite.

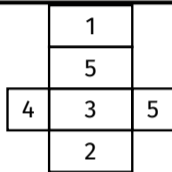
# Start Tasks - Nets



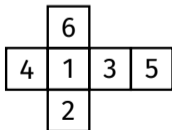
1. How many faces does this cube net have?



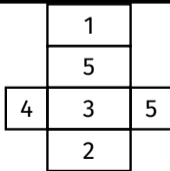
3. Does this T-shape form a cube when folded?



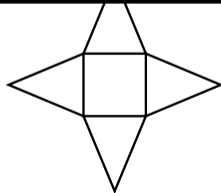
5. What 3D shape does this net form?



2. When folded, which face is opposite face 2?

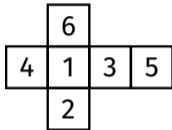


4. How many faces does a



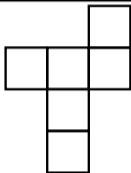
6. How many faces does

# Start Tasks - Nets



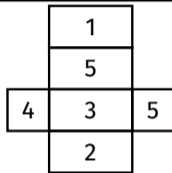
1. Faces in this net?

6



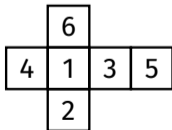
3. Does T form a cube?

Yes



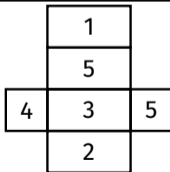
5. What 3D shape?

Cuboid

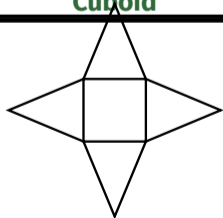


2. Opposite face 2?

Face 5

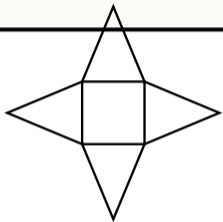


4. Faces of a cuboid?

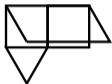


6. Pyramid faces?

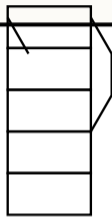
# Start Tasks - Nets



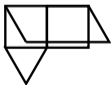
7. What shape do the



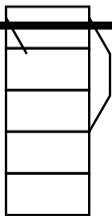
9. How many rectangular faces?



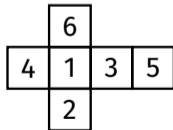
11. How many rectangular



8. How many faces on a triangular prism?

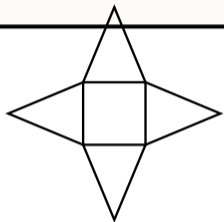


10. How many faces on a

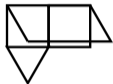


12. How many different cube nets are possible?

# Start Tasks - Nets

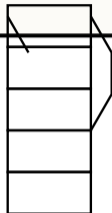


7. Triangles meet at?

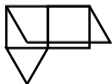


9. Rectangular faces?

3

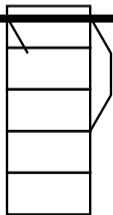


11. Rectangular faces in net?

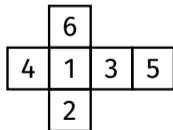


8. Triangular prism faces?

5



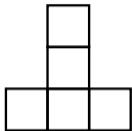
10. Hex prism faces?



12. Distinct cube nets?

11

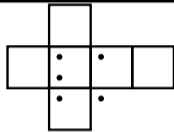
# Start Tasks - Nets



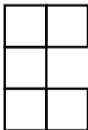
13. Can this pentomino fold into an open box?



15. How many faces on a tetrahedron?



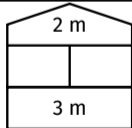
17. On a standard die, what do opposite faces sum to?



14. Can this pentomino form an open box?

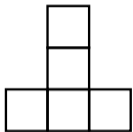


16. What shape are the faces?



18. How many triangular faces does this tent net

# Start Tasks - Nets



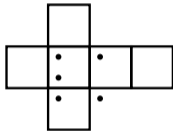
13. Open box from A?

Check by folding



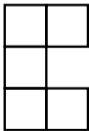
15. Tetrahedron faces?

4



17. Opposite faces sum?

7



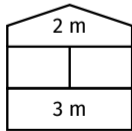
14. Open box from B?

Check by folding



16. Face shape?

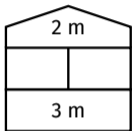
Triangle



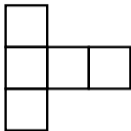
18. Triangular faces?

2

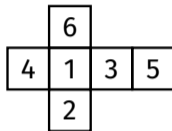
# Start Tasks - Nets



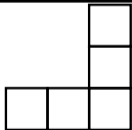
19. How many faces total on this tent net?



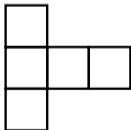
21. This net has 5 faces. What is missing?



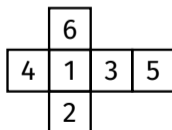
23. Name the 3D shape this net forms.



20. Will this 5-square L-shape form an open

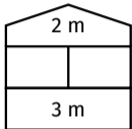


22. How many faces will this open box have?



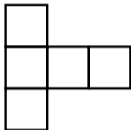
24. What shape is each face of a cube?

# Start Tasks - Nets



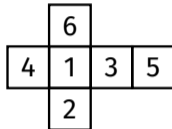
19. Total faces?

5



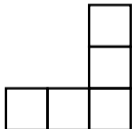
21. Missing what?

The lid / top face



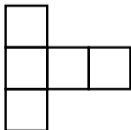
23. 3D shape name?

Cube



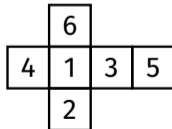
20. Open box from L?

Check by folding



22. Faces when folded?

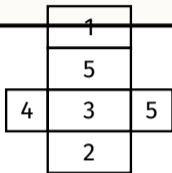
5



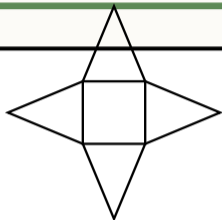
24. Shape of each face?

Square

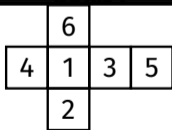
# Start Tasks - Nets



**25. A cuboid has 6 faces.  
How many different-sized**

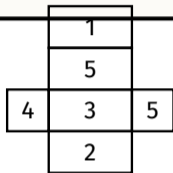


**27. Sketch a different  
valid net for a square  
pyramid.**



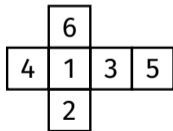
**26. Sketch this net on  
paper. Label the face that**

# Start Tasks - Nets

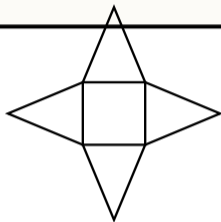


25. Different-sized face pairs?

3 pairs



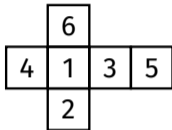
26. Sketch and label opposite face 1.



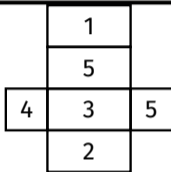
27. Different pyramid net?

e.g. 4 triangles in a row

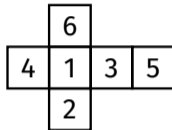
# Build Tasks - Nets and SA



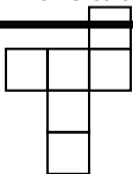
1. Which face is opposite face 3 in this cube net?



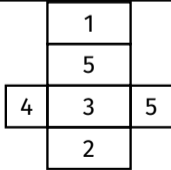
3. Cuboid 5 cm x 3 cm x 2 cm. Volume?



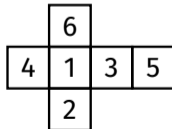
5. Cube side 4 cm. Volume?



2. In the T-net, which face is opposite the top?

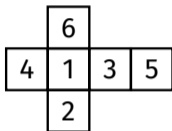


4. Surface area of the



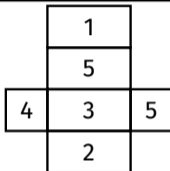
6. Surface area of a 4 cm cube?

# Build Tasks - Nets and SA



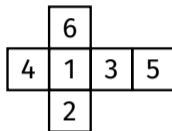
1. Opposite face 3?

Face 4



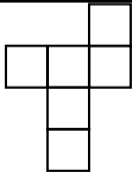
3. Volume  $5 \times 3 \times 2$ ?

$30 \text{ cm}^3$

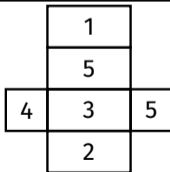


5. Cube side 4, volume?

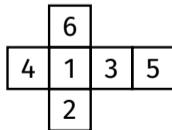
$64 \text{ cm}^3$



2. Opposite top square?



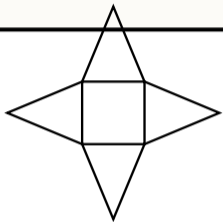
4. Surface area?



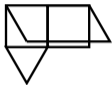
6. Surface area  $4 \text{ cm}^2$ ?

$96 \text{ cm}^2$

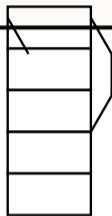
# Build Tasks - Nets and SA



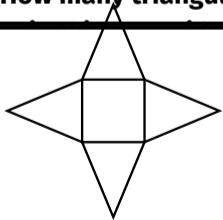
7. How many triangular



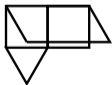
9. Equilateral triangle  
sides 2 cm, length 4 cm.  
Volume?



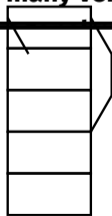
11. How many vertices on



8. How many edges on a

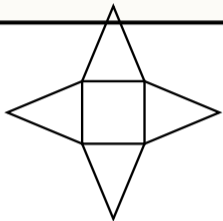


10. Surface area of the  
prism?

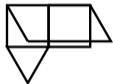


12. How many edges on a

# Build Tasks - Nets and SA

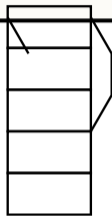


7. Triangles in pyramid?

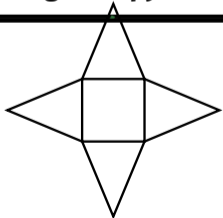


9. Volume 2 cm tri + 4 cm?

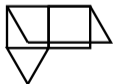
6.92 cm<sup>3</sup>



11. Hex prism vertices?

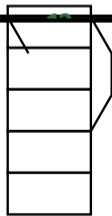


8. Pyramid edges?



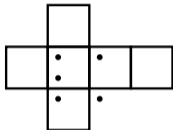
10. Surface area?

27.46 cm<sup>2</sup>

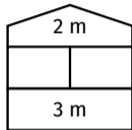


12. Hex prism edges?

# Build Tasks - Nets and SA



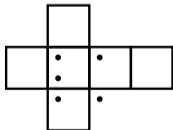
13. If 1 faces up, what is on the bottom?



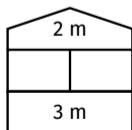
15. Tent floor 3 m by 4 m.  
Floor area?



17. How many vertices on a tetrahedron?



14. If 3 faces you, which face is opposite?

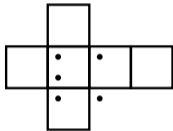


16. Which faces form the tent floor?



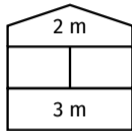
18. How many edges on each face?

# Build Tasks - Nets and SA



13. 1 up = bottom?

6



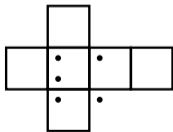
15. Floor area  $3 \times 4$ ?

$12 \text{ m}^2$



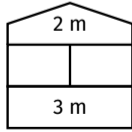
17. Tetrahedron vertices?

4



14. 3 facing = opposite?

4



16. Floor faces?

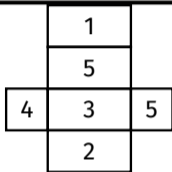
Large rectangle



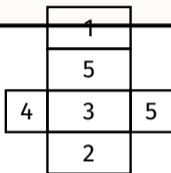
18. Edges per face?

3

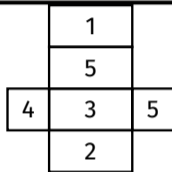
# Build Tasks - Nets and SA



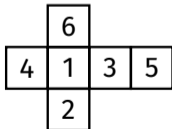
19. How many  $1 \times 1 \times 1$  cubes fit in a  $5 \times 3 \times 2$  box?



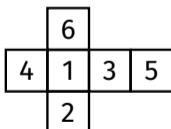
21. Gift box  $12 \times 5 \times 3$  cm.  
Cardboard needed



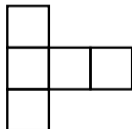
23. Rectangular prism  
 $10 \times 4 \times 2$  m. Surface area?



20. A cube has surface area  $54 \text{ cm}^2$ . Side length?

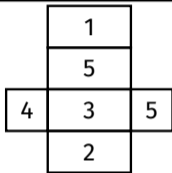


22. Cube face area  $25 \text{ cm}^2$ . Total SA?



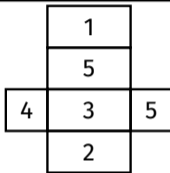
24. Open box has 5 faces.  
If cube of side 3, SA?

# Build Tasks - Nets and SA



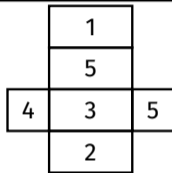
19. Cubes in  $5 \times 3 \times 2$ ?

30



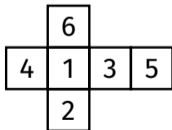
21.  $12 \times 5 \times 3$  cardboard?

$222 \text{ cm}^2$



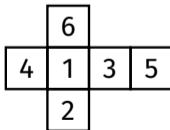
23.  $10 \times 4 \times 2$  prism SA?

$136 \text{ m}^2$



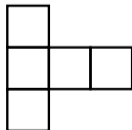
20. SA 54, side?

3 cm



22. Face  $25 \text{ cm}^2$ , total SA?

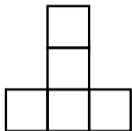
$150 \text{ cm}^2$



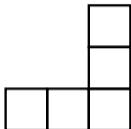
24. Cube side 3, open SA?

$45 \text{ cm}^2$

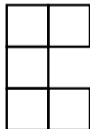
# Build Tasks - Nets and SA



**25. Pentomino A: valid cube net?**

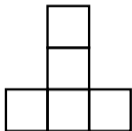


**27. L pentomino: can it fold to an open box?**



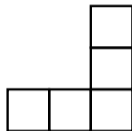
**26. Pentomino B: valid cube net?**

# Build Tasks - Nets and SA



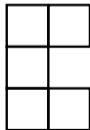
25. Valid cube net?

Check by folding



27. Open box from L?

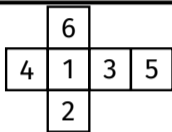
Check by folding



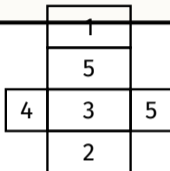
26. Valid cube net?

Check by folding

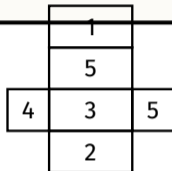
# Push Tasks - Nets and SA



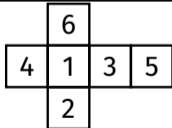
1. Name 3 arrangements of 6 squares that do NOT fold to a cube.



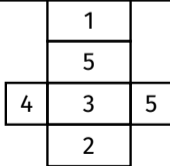
3. A  $5 \times 3 \times 2$  cuboid has 3 pairs of opposite faces.



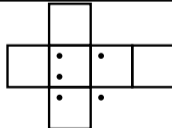
5. Which dimensions give maximum SA for volume



2. Explain why some cross shapes of 6 squares

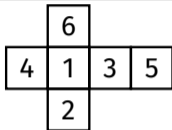


4. Minimise SA for volume

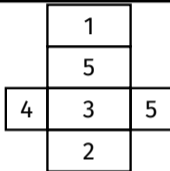


6. Prove that opposite faces of a standard die

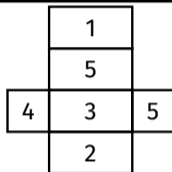
# Push Tasks - Nets and SA



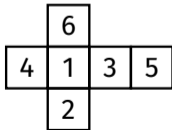
1. Invalid arrangements?  
e.g. 4 in a row with 2 on  
same side



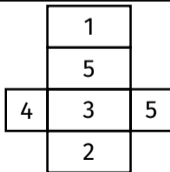
3. 3 pairs face areas?  
15, 10, 6 each x 2



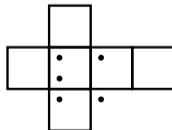
5. Max SA for  $V=96$ ?  
 $1 \times 1 \times 96 = 386 \text{ cm}^2$



2. Why some fail?  
Overlan when folded

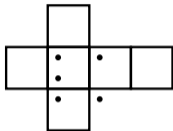


4. Min SA for  $V=96$ ?

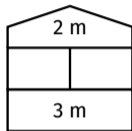


6. Opposite sums to 7?  
Standard: 1-6 2-5 3-4

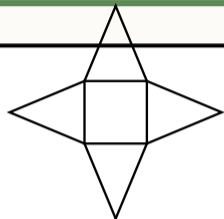
# Push Tasks - Nets and SA



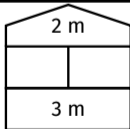
7. Design a different die net with 1 opposite 6.



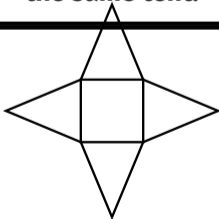
9. Draw a different net for the same tent.



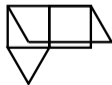
11. Pyramid base area  $25 \text{ cm}^2$  each triangle area  $15$



8. Explain why tent triangular faces are

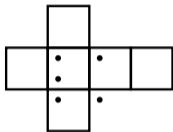


10. Draw all 4 triangles



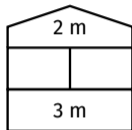
12. Draw the net of a right-triangle prism.

# Push Tasks - Nets and SA



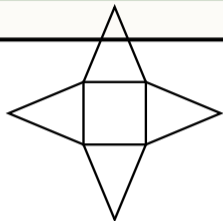
7. Different die net?

Any valid cube net

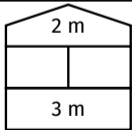


9. Different net?

Swap triangle positions

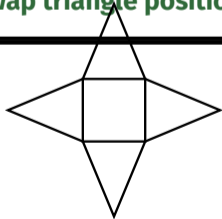


11. Pyramid SA: base 25,  
tri 15 each?

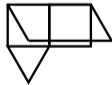


8. Triangles isosceles?

Two equal sides by



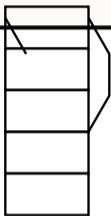
10. Triangles congruent?



12. Right triangle prism  
net?

Rectangles + 2 triangles

# Push Tasks - Nets and SA



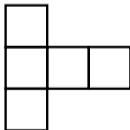
13. Find SA of hex prism:



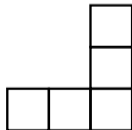
15. Why must a tetrahedron net use 4 triangles?



14. How many distinct nets for a tetrahedron?

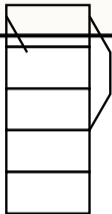


16. Open box volume  $12 \text{ cm}^3$  SA (no top)?



18. L pentomino can form a cube net if explain

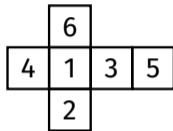
# Push Tasks - Nets and SA



13. Hex prism SA side 2,  
len 5?



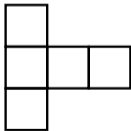
15. Why 4 triangles?  
4 triangular faces



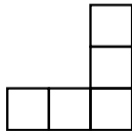
17. Shortest surface path?  
Unfold net, draw line



14. Tetrahedron nets?  
2 distinct nets

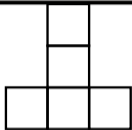


16.  $V=12$  no top SA?  
Depends on dimensions

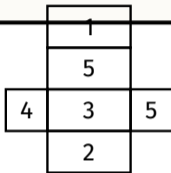


18. L as cube net?  
Only with 6th square

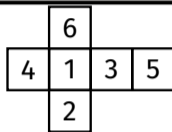
# Push Tasks - Nets and SA



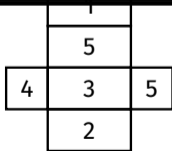
19. Only 2 of 12 pentominoes cannot form an open box. Which?



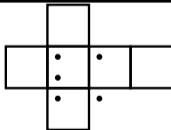
21.  $4 \times 6 \times 4$  cuboid uses least paper for  $V=96$ .



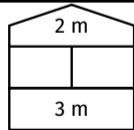
23. Shortest path: unfold the net, draw straight line.



20.  $1 \times 1 \times 96$  cuboid uses most wrapping paper

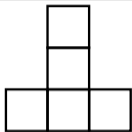


22. Minimum colours to paint a cube so adjacent



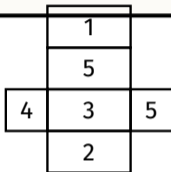
24. Ribbon on tent box: 4 m total, knot 20 cm.

# Push Tasks - Nets and SA



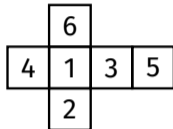
19. 2 non-box pentominoes?

I and X pentominoes



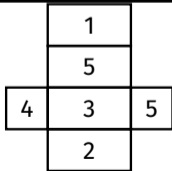
21. 4x6x4 min paper proof?

*Closest to cube*

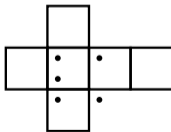


23. Shortest path?

Draw net, straight line

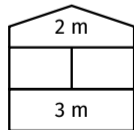


20. 1x1x96 max paper?



22. Min colours?

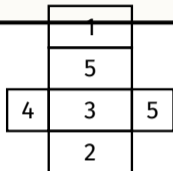
3 (opposite faces same)



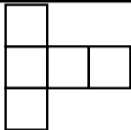
24. Ribbon on faces?

3.8 m on faces

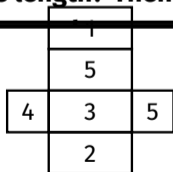
# Push Tasks - Nets and SA



25. Cube SA =  $150 \text{ cm}^2$ .  
Side length? Then find

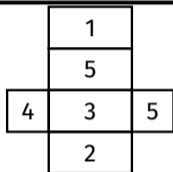


27. Open-top box from  
 $6 \times 4 \text{ cm}$  card. Max  
volume?



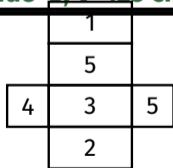
26. Cuboid  $8 \times 3 \times 2 \text{ cm}$ . Find  
the cost to wrap at  $\$0.05$

# Push Tasks - Nets and SA

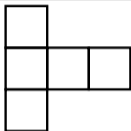


25. SA=150, side then V?

Side=5, V=125 cm<sup>3</sup>



26. 8x3x2 wrap cost  
\$0.05/cm<sup>2</sup>?



27. Open-top max  
volume?

Depends on card size